



11th International Conference on Multiphase Flow, Kobe Japan

Coalescence and breakup of droplets in a viscoelastic turbulent fluid

Ianto Cannon and Marco E. Rosti

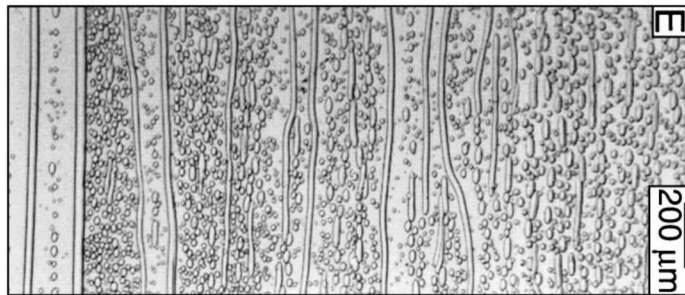
Complex Fluids and Flows Unit, Okinawa Institute of Science and Technology, Japan



Droplets in viscoelastic flows

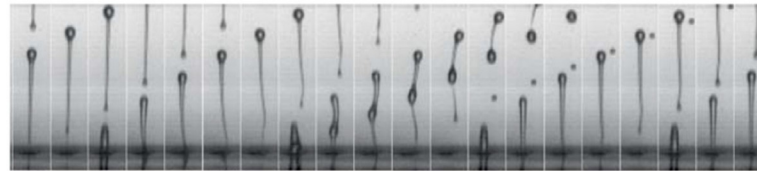
- Ubiquitous industry and nature

Polymer production



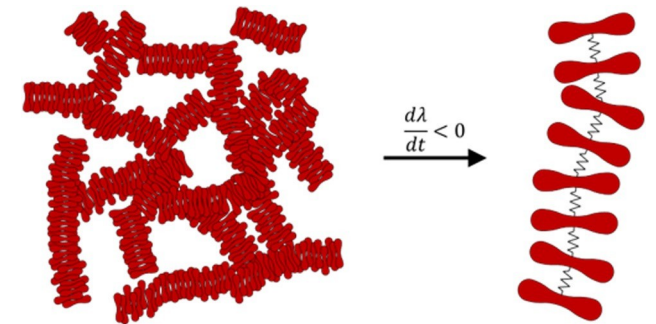
K. B. Migler, 'String Formation in Sheared Polymer Blends: Coalescence, Breakup, and Finite Size Effects', *Phys. Rev. Lett.* 2001

Inkjet printing



H. Wijshoff, 'Drop dynamics in the inkjet printing process' *Curr. Opin. Colloid Interface Sci.* 2018

Blood

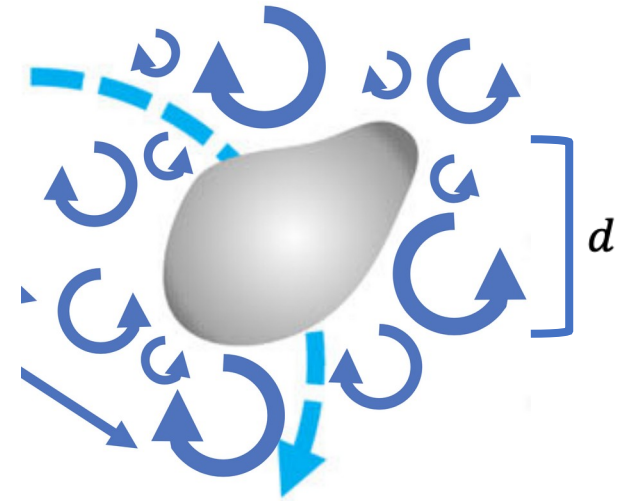


J. S. Horner et al. 'Measurements of human blood viscoelasticity and thixotropy...'. *J. Rheol* 2019

Drop size spectrum in Newtonian flows

- Deane & Stokes (*Nature* 2002) and Cialesi-Esposito et al. (*Commun Phys* 2023) observed a $N \sim d^{-10/3}$ dependence on drop diameter d in the drop size spectrum for droplets in turbulence.
- Garrett et al (*J. Phys. Oceanogr* 2000) proposed a mechanism;
- Drops of diameter d experience velocity fluctuations of order $(\varepsilon d)^{1/3}$, causing breakup in time $d(\varepsilon d)^{-1/3} \sim d^{2/3}$.
- We suppose that it is broken into two drops of equal diameter $2^{-1/3}d$
- These persist for a time $(2^{-1/3}d)^{2/3}$.
- Given the reduced lifetime, we expect $2(2^{-1/3})^{2/3} = 2^{7/9}$ times as many drops of this size.
- Divide by the ratio of the drop diameters to get the number per unit radius;
 $N(2^{-1/3}d) = 2^{1/3}2^{7/9}N(d) = 2^{10/9}N(d)$.
- This gives the observed scaling $N(d) = d^{-10/3}$.

$$d_H = 0.725 \left(\frac{\sigma^2}{\rho^2 \varepsilon^3} \right)^{1/5}$$



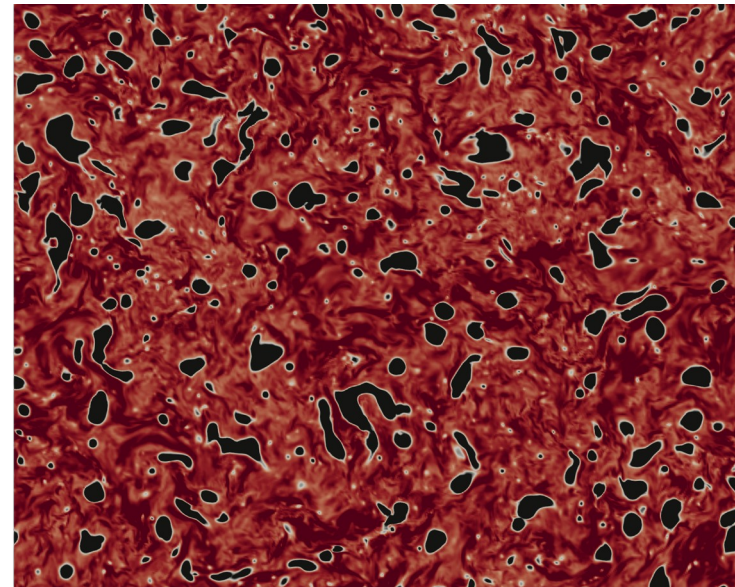
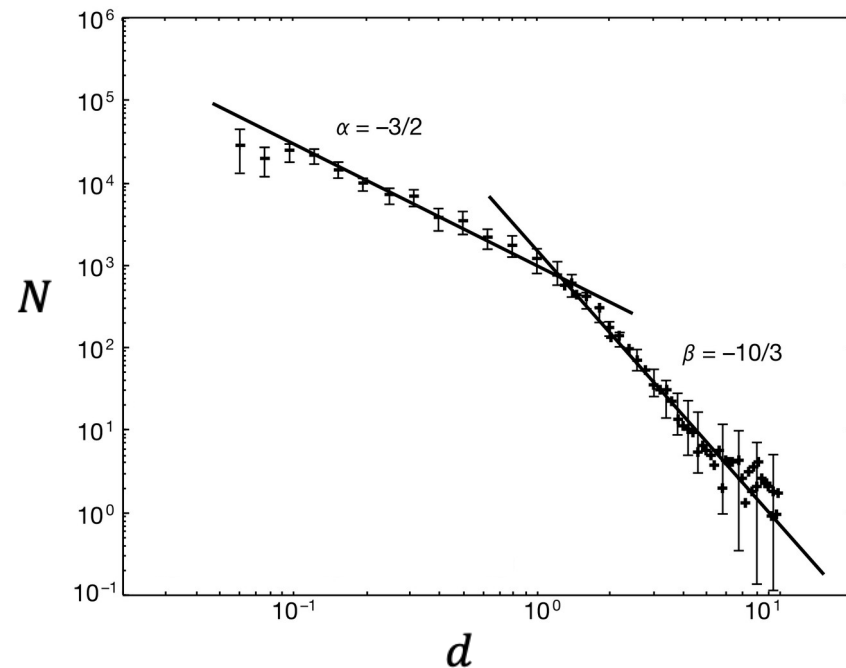
Qi et al. Fragmentation in turbulence by small eddies. *Nat Commun* (2022).



Goal of the work

- Previous investigations of drop breakup have been carried out in the classical Kolmogorov cascade.

How is droplet breakup affected by non-classical turbulence?



Deane & Stokes. Scale dependence of bubble creation mechanisms in breaking waves. *Nature* (2002).



Numerical method

Flow equations are solved on a 500^3 grid with **triperiodic boundary conditions**.
Turbulence is sustained by stochastic forcing (**Eswaran & Pope, *Comput. Fluids*, 1988**)

$$\rho_f \left(\frac{\partial u_\alpha}{\partial t} + \frac{\partial u_\alpha u_\beta}{\partial x_\beta} \right) = - \frac{\partial p}{\partial x_\alpha} + \frac{\partial}{\partial x_\beta} \left(2\mu_f S_{\alpha\beta} + \frac{\mu_p}{\tau_p} C_{\alpha\beta} \right) + F_\alpha \quad \frac{\partial u_\alpha}{\partial x_\alpha} = 0$$

Dimesionless groups

$$Re_\lambda \equiv \rho u_{rms} / \mu_f \approx 200,$$

Oldroyd-B model

$$\frac{\partial C_{\alpha\beta}}{\partial t} + u_\gamma \frac{\partial C_{\alpha\beta}}{\partial x_\gamma} = C_{\alpha\gamma} \frac{\partial u_\beta}{\partial x_\gamma} + C_{\gamma\beta} \frac{\partial u_\gamma}{\partial x_\alpha} - \frac{C_{\alpha\beta} - \delta_{\alpha\beta}}{\tau_p}$$

$$0 < De \equiv \tau_p / \tau_L < 3$$

$$\tau_L = L / u_{rms}$$

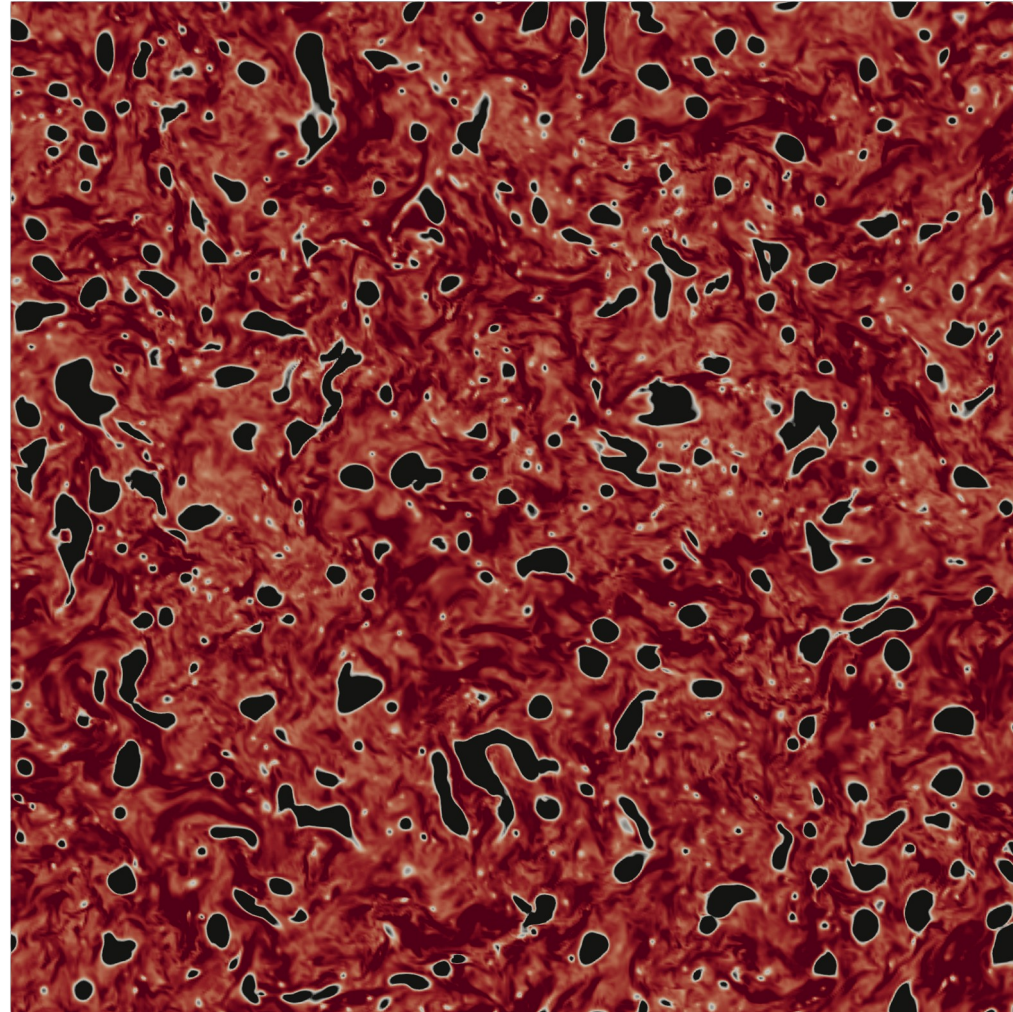
Volume-of-fluid model (**Ii et al. *J. Comput. Phys.* 2012**)

$$\partial_t \phi + \partial_i u_i \mathcal{H} = \phi \partial_i u_i, \quad F_\alpha = \sigma \xi \delta_s n_\alpha$$

$$\Phi = \{0, 0.1\}$$

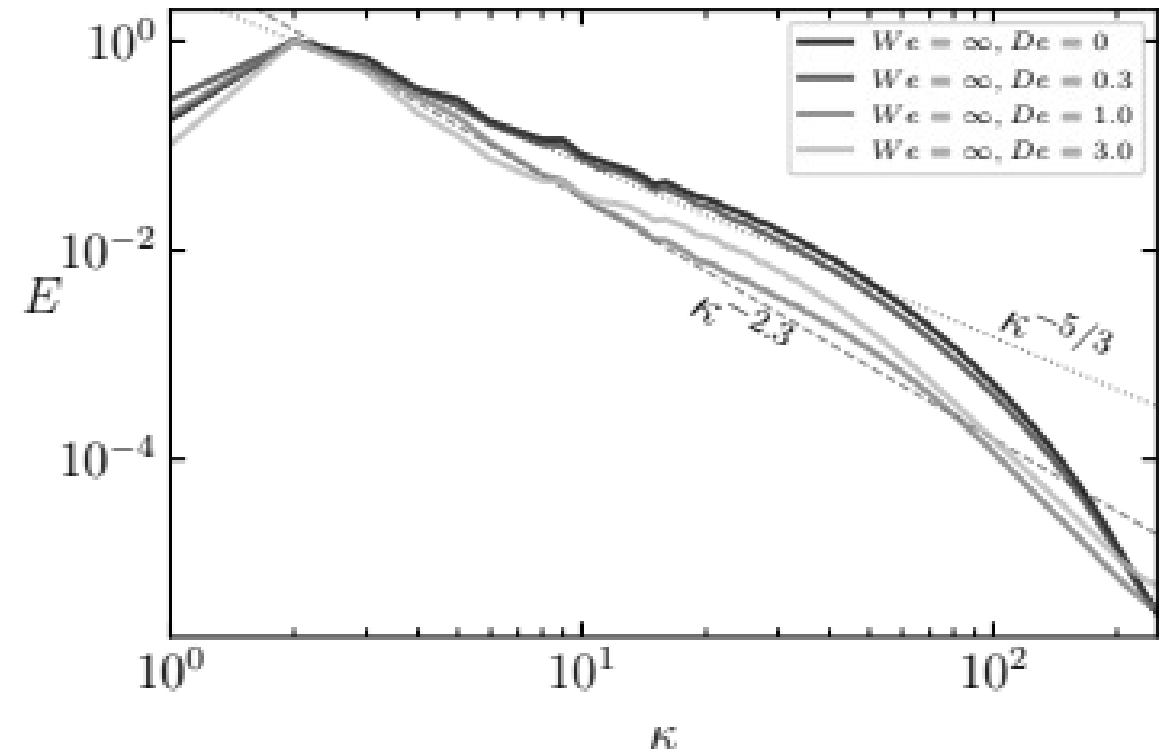
$$We_{\mathcal{L}} = \rho_c \mathcal{L} u_{rms}^2 / \sigma = \{20, 40\}$$

Droplets in a viscoelastic carrier fluid



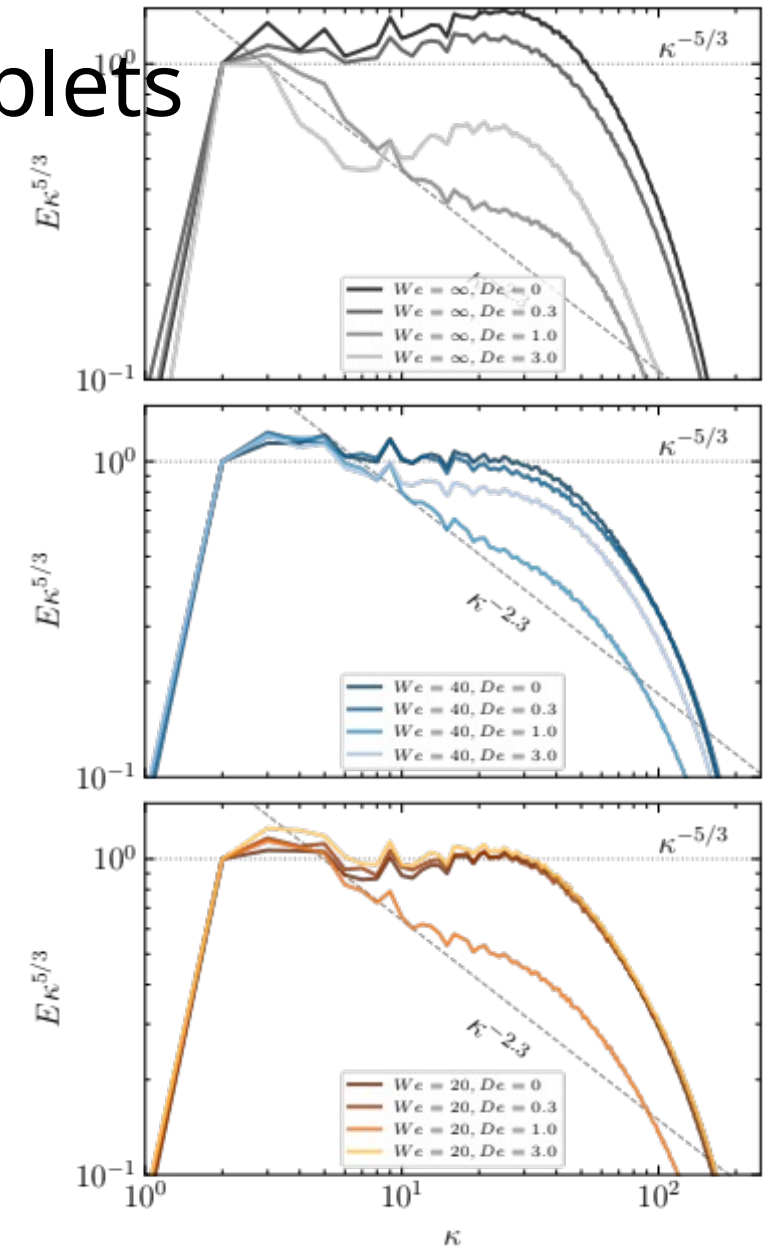
Turbulence modulation due to the viscoelastic fluid

- For the Newtonian single phase flow we observe the classical $E \sim \kappa^{-5/3}$ scaling
- In the case of $De = 1$, the viscoelastic fluid introduces a new scaling $E \sim \kappa^{-2.3}$
- This has been previously observed by Rosti Perlekar & Mitra. (Large is different.... *Science Advances* 2023).



Turbulence in the presence of droplets

- The droplets have little effect on the kinetic energy spectrum of the fluid.
- As before, $E \sim \kappa^{-2.3}$ for the $De = 1$ cases.

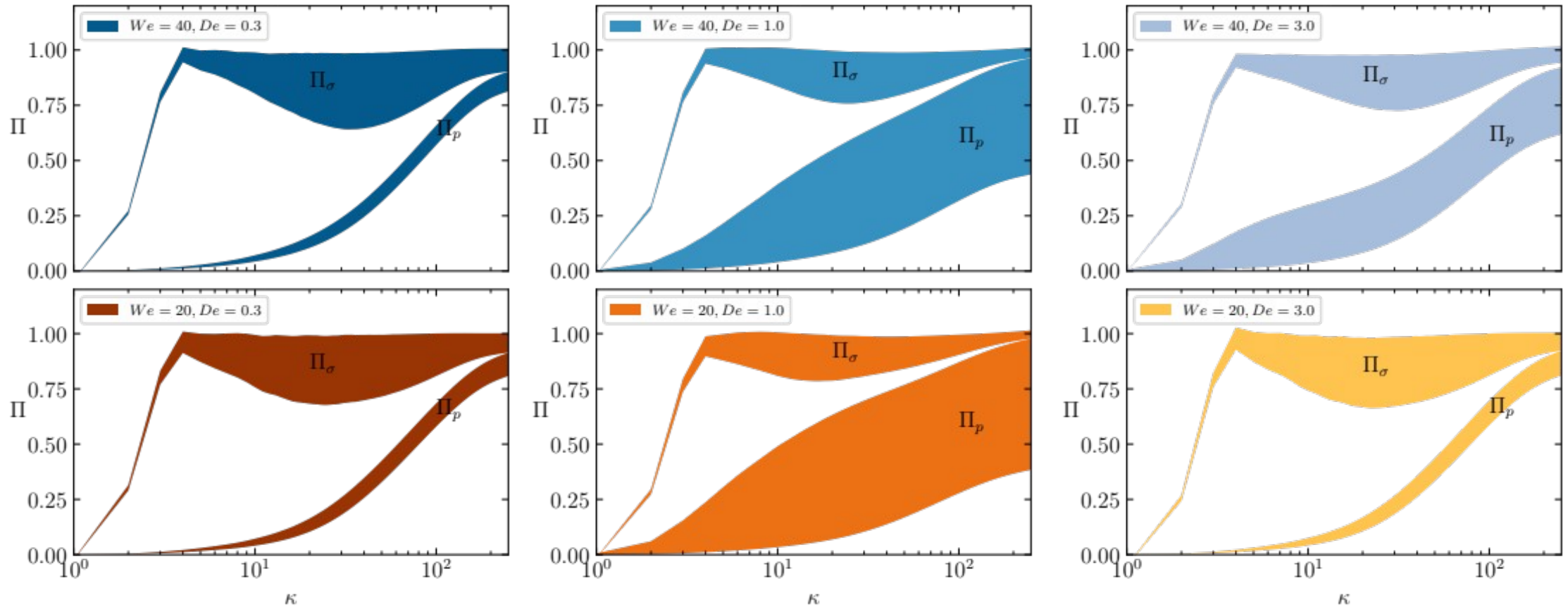


Spectral energy balance

$$\epsilon = P + \Pi_\sigma + \Pi + \Pi_p + D$$

injection
convection
dissipation

De

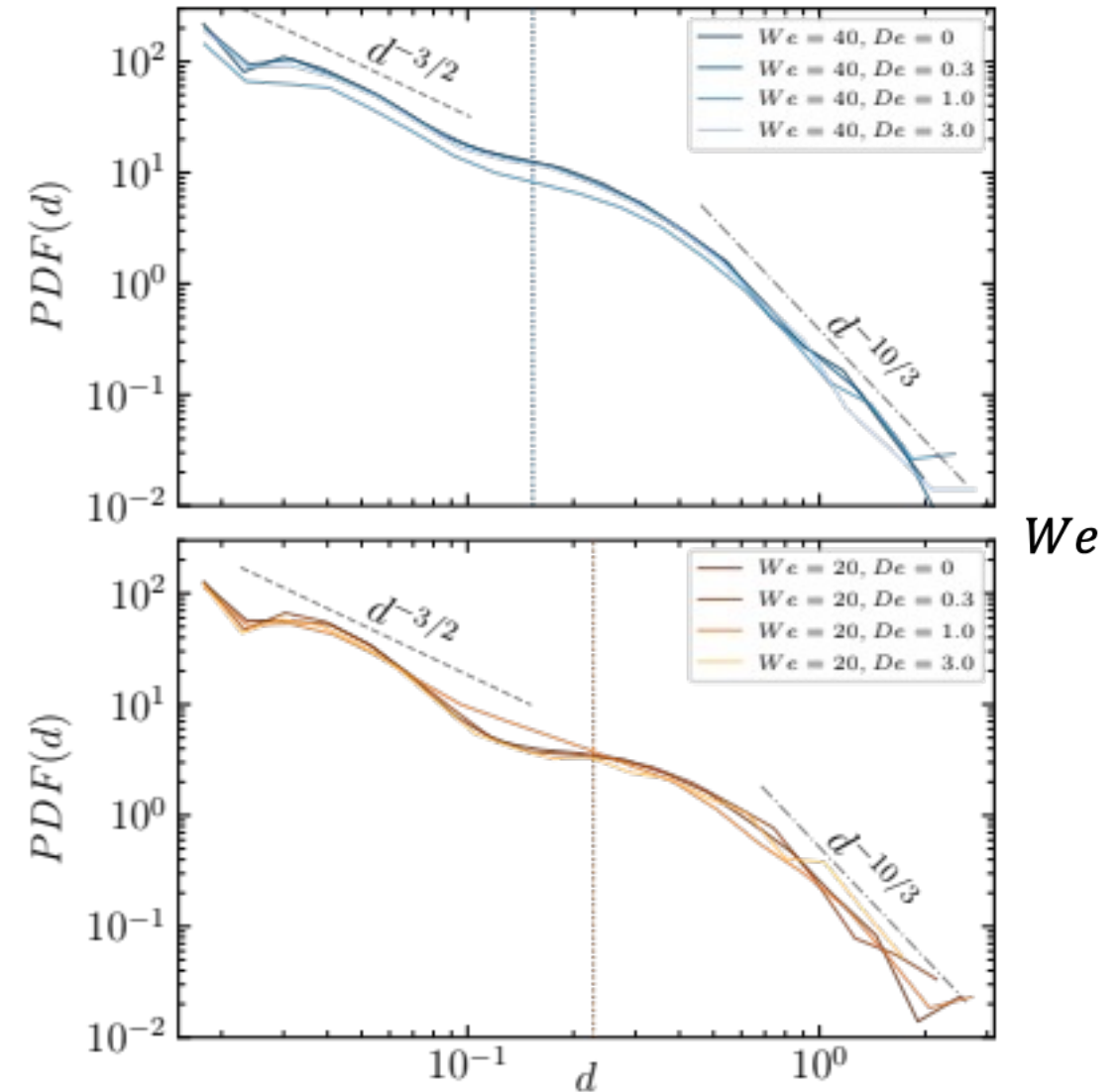


We



Drop size spectrum

- At larger Weber numbers, there are more small drops, supporting the previous observation that Π_σ moves to larger wavenumbers.
- The mechanism of [Garrett et al \(J. Phys. Oceanogr 2000\)](#) with $E \sim \kappa^{-2.3}$ predicts a drop size scaling of $d^{-3.65}$ in the breakup region.
- However, we recover $d^{-3/2}$ and $d^{-10/3}$ scalings in the drop size spectra at all Deborah numbers.



Conclusions and further work

- We made DNS of droplet breakup in viscoelastic turbulence. We found:
 - An energy scaling $E \sim \kappa^{-2.3}$ is seen at intermediate Deborah numbers
 - Increasing the Weber number reduces the drop size, and the interface coupling acts at larger wavenumbers.
 - The canonical droplet size scalings are recovered, even in the presence of a turbulent viscoelastic fluid.
 - To better elucidate the breakup mechanism, we should measure drop size spectra in other flows, such as elastic turbulence, linear forcing, 2D turbulence, and bubble induced turbulence.

